

Objectives: You learn how to completely factor polynomials in $x^2 + bx + c$ form.

Factoring When Terms Have a Common Factor (GCF factoring)

Find what they have in common and use the reverse of the distributive property!!

Example 1: Factor the following.

a) $\frac{15x^2}{15} + \frac{15}{15}$
 $15(x^2 + 1)$

Sep 23-4:17 PM

b) $\frac{24x^2}{6x} + \frac{30x}{6x}$
 $6x(4x + 5)$

Apr 28-10:05 AM



Factoring By Grouping

Group together pairs that have something in common, then use the reverse of the distributive property!!

4 terms!

Example 2: Factor $2x^3 + 10x^2 + x + 5$
 $2x^2(x+5) + 1(x+5)$
 $(x+5)(2x^2+1)$

Sep 23-4:19 PM

Example 3: Factor $[ax + by] + ay + bx$

$[ax+ay] + [bx+by]$
 $a(x+y) + b(x+y)$
 $(x+y)(a+b)$

Sep 23-4:19 PM

Example 4: Factor $7x^3 - 2x^2 - 7x^2 + 2x$
 $x^2(7x-2) - x(7x-2)$
 $(7x-2)(x^2-x)$
 $x(7x-2)(x-1)$



Sep 23-4:20 PM

Factoring Trinomials $x^2 + bx + c$

Example 5: Factor $x^2 + 5x + 6$

Pairs of Factors of 6	That SUM to 5
1,6	
3,2	

Check by multiplying by FOIL!

$(x+3)(x+2)$
 $x^2 + 2x + 3x + 6$

Sep 23-4:20 PM

Example 6: Factor

$$a) y^2 - 8y + 12 \begin{matrix} 3,4 \\ -6,2 \\ 1,12 \end{matrix}$$

$$(y-6)(y-2)$$

Sep 23-4:23 PM

$$b) x^2 - 6x + 5 \begin{matrix} 1,5 \\ (x-1)(x-5) \end{matrix}$$

Apr 28-10:06 AM

Example 7: Factor

$$a) x^2 + 3x - 4 \begin{matrix} 4,-1 \\ (x+4)(x-1) \end{matrix}$$

Sep 23-4:23 PM

$$b) x^2 + 15x - 34 \begin{matrix} -2, 17 \\ (x-2)(x+17) \end{matrix}$$

Mar 30-1:51 PM

Example 8: Factor

$$a) x^2 - 6x - 7 \begin{matrix} -7, 1 \\ (x-7)(x+1) \end{matrix}$$

Sep 23-4:25 PM

$$b) t^2 - 24 + 5t$$

→ First, rewrite in descending order

$$t^2 + 5t - 24 \begin{matrix} -3, 8 \\ (t-3)(t+8) \end{matrix}$$

Apr 28-10:08 AM

Factoring Trinomials $ax^2 + bx + c$: Using the AC Method

Example 9: $2x^2 - x - 1$

1. Multiply a & c

-2

$a =$	2
$c =$	-1
$ac =$	-2

2. Find 2 numbers that are factors of ac and add to b

must -2 adds to -1 $-2, 1$

3. "Un-combine like terms" for your b -term

$2x^2 - x - 1$
 $2x^2 - 2x + x - 1$

4. Use grouping to finish your factoring

$[2x^2 - 2x] + [x - 1]$
 $2x(x-1) + 1(x-1)$
 $(x-1)(2x+1)$

5. Check your answer:

$(x-1)(2x+1)$
 $2x^2 + x - 2x - 1$

Feb 15-9:39 AM

Example 10: Factor

a) $3x^2 - x - 2$
 $ac = -6$
 $-3, 2$
 $[3x^2 - 3x] + [2x - 2]$
 $3x(x-1) + 2(x-1)$
 $(x-1)(3x+2)$

Sep 27-8:57 AM

b) $5x^2 + 22x + 8$

$ac = 40$
 $20, 2$

$[5x^2 + 20x] + [2x + 8]$
 $5x(x+4) + 2(x+4)$
 $(x+4)(5x+2)$

Sep 27-8:57 AM

Factoring Difference of Squares

Recall: $(x+2)(x-2) = x^2 - 2x + 2x - 4$
 $x^2 - 4$

The product above is called a difference of squares because it is the subtraction of two perfect squares.

Sep 27-8:58 AM

Example 11: $x^2 - 16$

$(x+4)(x-4)$

Sep 27-8:59 AM

Example 12: $x^2 - 49$

$(x+7)(x-7)$

Sep 27-9:00 AM

Example 13: $36 - x^2$

$$(b+x)(b-x)$$

Sep 27-9:00 AM

Feb 15-9:39 AM